

**UNIVERSITY COLLEGE LONDON**

University of London

**EXAMINATION FOR INTERNAL STUDENTS**

For The Following Qualifications:–

*B.Sc.*    *M.Sci.*

**Astronomy 2B17: Physics of the Solar System**

COURSE CODE        : **ASTR2B17**

UNIT VALUE         : **0.50**

DATE                 : **19–MAY–04**

TIME                 : **14.30**

TIME ALLOWED      : **2 Hours 30 Minutes**

**Answer all SIX questions from section A and THREE questions from Section B.**  
The numbers in brackets indicate the provisional allocation of marks for each sub-section of the question.

Stefan-Boltzmann constant $\sigma$	$= 5.67 \times 10^{-8} \text{ W m}^{-2} \text{ K}^{-4}$
Boltzmann constant $k$	$= 1.38 \times 10^{-23} \text{ JK}^{-1}$
Proton mass $m_p$	$= 1.67 \times 10^{-27} \text{ kg}$
Electron mass $m_e$	$= 9.11 \times 10^{-31} \text{ kg}$
Electron charge $q$	$= -1.6 \times 10^{-19} \text{ C}$
Permeability of free space $\mu_0$	$= 4\pi \times 10^{-7} \text{ H m}^{-1}$
Mean Earth-Sun distance (1AU, Astronomical Unit)	$= 150 \times 10^6 \text{ km}$
Sun's radius $R_S$	$= 6.960 \times 10^8 \text{ m}$
Radius of Earth $R_E$	$= 6.37 \times 10^3 \text{ km}$
Radius of Mars $R_M$	$= 3.4 \times 10^3 \text{ km}$
Magnetic field at Earth's surface $B_E$	$= 31 \times 10^{-6} \text{ T}$

## Section A

- Describe what is meant by “primary”, “secondary” and “tertiary” crust. List reasons why there are a smaller number of meteor craters observed on the Earth compared with the moon. [8]
- Explain why the magnetic field of the solar wind is “frozen-in” and why, as a consequence, in the ecliptic plane the mean angle of the interplanetary magnetic field with respect to the Sun-Earth line is around  $45^\circ$ . [6]
- The simple heat balance equation for the effective temperature of a planet is given by the following equation:

$$T_p^4 = \frac{(R_s^2 T_s^4)(1 - A)}{k r_p^2}$$

Define all the terms and briefly explain the theory behind the derivation of this equation. Give two examples of planets to illustrate different  $k$  values. [6]

- Explain qualitatively why the adiabatic lapse rate determines the stability of an atmosphere. Account for why the adiabatic lapse rate of Mars should differ from that of Earth. [7]

5. Explain what is meant by the  $J$  parameters and how they may help determine the interior composition of a planet [6]
6. Derive an expression for the Larmor radius  $r$  for a particle with charge  $q$  in a magnetic field  $B$ . Calculate the values of  $r$  for the following particles using the given parameters:
- An electron in the solar wind, where  $B = 6\text{nT}$  and the solar wind temperature =  $8.9 \times 10^4\text{K}$ .
  - A  $7\text{keV}$  electron travelling with a pitch angle of  $60^\circ$  to the Earth's magnetic field where the field value is  $240\text{nT}$ .
- [7]

### Section B

7. Theories of the formation of the Solar System must account for the observations of geometry, dynamics and chemistry of the Sun and planetary bodies. List 5 observations that must be accounted for. [5]

Explain what the condensation sequence is, giving appropriate examples. [6]

A homogeneous spherical primordial nebula with radius  $R_0$  collapses to form a homogeneous disk-shaped solar system with radius  $R_1$  and depth  $d$ . Assume a rigid sphere such that all parts of the sphere rotate about a single axis through its centre with angular speed  $\omega_0$ , and similarly a rigid disk that rotates with angular speed  $\omega_1$  about a single axis through its centre. Determine the moment of inertia of the disk-shaped solar system in terms of its mass  $M$  and then determine the moment of inertia of the spherical solar nebula in terms of its mass  $M$ .

Show that the ratio of the angular speeds  $\omega_0 / \omega_1$  is given by:

$$(\omega_0 / \omega_1) = (5/4)(R_1 / R_0)^2$$

[Hint: the moment of inertia of a disk may be determined by considering an elemental ring of radius  $r$ , thickness  $dr$  and depth  $d$ . The moment of inertia of a sphere may be determined by considering an elemental disk of radius  $r$  and depth  $dz$  that is a distance  $z$  from the centre of the sphere.] [9]

8. Sketch and label a diagram of a comet as it nears the Sun. Account for why a comet close to the Sun has a different appearance to when it is in the outer reaches of the solar system. [8]

Briefly explain how the trajectories and periodicity of comets indicate where their origins may lie. [6]

A spacecraft approaches and lands on a comet. The spacecraft uses a spring to lift off from the comet surface. On Earth the spring is able to lift the spacecraft to a height of 3m. What is the largest cometary nucleus that the spacecraft could escape from? (Assume that the ratio of the densities of the Earth to the comet is 5:1.) [6]

9. Explain qualitatively how the radius of a stable orbit for a planetary satellite is restricted by both the Roche Limit and the Instability Limit. Give a simple derivation of the Roche Limit to show that it can be given by the following expression, where  $C$  is a constant, and explain all the parameters.

$$r = C (\rho_p / \rho_s)^{1/3} R_p \quad [9]$$

Describe the general structure of rings and satellites around the Gas Giants and include an account of how the Roche Limit might influence the geometry and distribution of this matter. [11]

10. Describe how the distribution of sunspots changes during the sunspot cycle. Explain why there is an 11 year and 22 year cycle for sunspots. How it is possible to distinguish a sunspot at the end of the old cycle from one at the beginning of a new cycle? Describe the magnetic field model that accounts for sunspots and the sunspot cycle. [13]

Briefly describe each component of the process that links a coronal mass ejection with the Earth's auroral regions and leads through to the shutdown of the electricity grid in northern Canada. [7]

11. Briefly describe the mechanisms of differentiation in the formation of a planet. [6]

Compare and contrast, with diagrams, the possible internal structures of Earth and Venus. [11]

Give 3 possible reasons why Earth has a magnetic field, while Venus has none. [3]